

## SUBJECT : CHARACTERISTIC FUNCTION AND HIS MOMENTS, REVERSAL FORMULAS

B. Makhmudov

Kokand DPI is a Mathematician Department Assistant, Teacher

### ABSTRACT

This A characteristic function in the article is an independent one central limit theorems of uniformly distributed randomness, theorems of Lindeberg, Feller and Lyupanov, some limit theorems of random branching process, theorems about the rate of approximation to the exponential distribution law and their proofs are considered.

### Annotation

In this article deals with the characteristic function, the theorems of randomly distributed central limits of independent distribution, the theorems of Lindeberg , Feller and Lyupanov , some limit theorems of random branching process, theorems on the estimation of the rate of approach to the exponential distribution law and their proofs.

### Higher order moments .

Random of quantities another numerous also referring to the characteristics let 's go Such characteristics as a lot cases high in order moments is used .

If  $\xi$  the distribution function of a random variable is  $F(x)$ ,

$$m_k = \int_{-\infty}^{\infty} x^k dF(x) = E\xi^k, \quad k \geq 0 \tag{1.1}$$

integral  $k$  - order random variable moment or  $k$  - order initial moment is called Of course , if

$$E|\xi|^k = \beta_k = \int_{-\infty}^{\infty} |x|^k dF(x) < \infty \tag{1.2}$$

integral approximant be  $k$  - ordered  $m_k$  moment will exist ( $|m_k| \leq \beta_k$ ). Probabilities in theory  $m_k$

of torque that it exists  $\beta_k$   $k$  - order absolute torque is equal to the existing case .

If  $\xi$  distribution function of random variables  $F(x)$  is of discrete type and its breakpoints

$$x_1, x_2, \dots, x_n, \dots$$

sequence organize if he does , then Stilts of the integral to the x axis according to  $k$  - order moment

$$m_k = \sum_{n=1}^{\infty} x_n^k P_n$$

equality with is determined. Here

$$P_n = F(x_n + 0) - F(x_n - 0) = F(x_n + 0) - F(x_n) = P(\xi = x_n)$$

being \_

$$\sum_{n=1}^{\infty} |x_n|^k P_n < \infty \tag{1.3}$$

assuming that the series converges to be done .

If  $\xi$  the distribution function of the random variable  $F(x)$  is of continuous type, and the function  $f(x)$  is its density function ( $F'(x) = f(x)$ ), then based on the property of the Stiltes integral

$$m_k = \int_{-\infty}^{\infty} x^k f(x) dx, \quad k \geq 0 \tag{1.4}$$

equality is determined by In this case

$$\int_{-\infty}^{\infty} |x|^k f(x) dx < \infty \tag{1.5}$$

integral assuming that it approaches will be done . The zeroth order moment is always there is and

$$m_0 = F(+\infty) - F(-\infty) = 1 .$$

First order moment

$$m_1 = \int_{-\infty}^{\infty} x dF(x) = E\xi \tag{1.6}$$

$\xi$  is the mean or mathematical expectation of a random variable . If  $c$  is a constant number ,

$$E(\xi - c)^k = \int_{-\infty}^{\infty} (x - c)^k dF(x) \tag{1.7}$$

Integral  $\int_{-\infty}^{\infty} (x - c)^k dF(x)$  is called *the k -order moment* of the random variable with respect to  $c$  . Mathematician don't wait relatively moments

$$\alpha_k = \int_{-\infty}^{\infty} (x - E\xi)^k dF(x) = E(\xi - E\xi)^k \tag{1.8}$$

$\alpha_k$  are called *k - order central moments* of the random variable .

Here  $(x - m_1)^k$  The expression is explained by Newton's binomial formula , as follows formulas harvest we do :

$$\begin{aligned} \alpha_0 &= 1, \quad \alpha_1 = 0, \\ \alpha_2 &= m_2 - m_1^2, \\ \alpha_3 &= m_3 - 3m_1m_2 + 2m_1^3, \\ \alpha_4 &= m_4 - 4m_1m_3 + 6m_1^2m_2 - 3m_1^4 \end{aligned}$$

and that's right . They are moments  $m_k$  of order  $k$  lar central moments  $\alpha_k$  connect with Immutable  $c$  to relatively second for the ordered torque

$$E(\xi - c)^2 = E[(\xi - m_1) + (m_1 - c)]^2 = \alpha_2 + (m_1 - c)^2 \geq \alpha_2$$

to the relationship have we will be and from him

$$\alpha_2 = \min_c E(\xi - c)^2 = E(\xi - m_1)^2 \tag{1.9}$$

equality we can It is known that this moment is random amount  $\xi$  is called the variance of and  $\xi$  from the main numerical characteristic for is considered Proof relation ( 1.9 ).  $\xi$  ng can be taken as the definition of the variance of a random variable .

If  $E\xi = 0$  if , the central moment is initial to the moment equal to will be

$\xi$  random of the amount  $k$  - order central absolute as the moment

$$E|\xi - E\xi|^k = \int_{-\infty}^{\infty} |x - E\xi|^k dF(x) \tag{1.10}$$

to expression it is said .

X ususan , if  $E\xi = 0$  is  $k$  - ordered \_ central absolute moment  $k$  - order initial with absolute torque on top of each other falls \_

### Higher order moments for inequalities

#### Cauchy-Buniakovsky inequality

Second in order to the moment has i x theory  $\xi$  and  $\eta$  random amounts for the following inequality suitable for :

$$E|\xi\eta| \leq \sqrt{E\xi^2} \cdot \sqrt{E\eta^2} \tag{1.11}$$

*Proof* . It is  $|\xi\eta| \leq \frac{1}{2}(\xi^2 + \eta^2)$  known that and  $E\xi^2$  and  $E\eta^2$  moments from its finiteness

$E|\xi\eta| < \infty$  that come comes out x and to the variables y depends has been positive determined this

$$E(x|\xi| + y|\eta|)^2 = x^2E\xi^2 + 2xyE(|\xi| \cdot |\eta|) + y^2E\eta^2$$

discriminant of the quadratic form

$$(2E(|\xi\eta|))^2 - 4E\xi^2E\eta^2 \leq 0$$

from which (1) the inequality holds since i arises.

#### Golder's inequality

Suppose 1 is probable with  $\xi \geq 0, \eta \geq 0$  va  $p, q$  let the relations for numbers

$$p > 1, q > 1, \frac{1}{p} + \frac{1}{q} = 1 \text{ be appropriate.}$$

If  $E\xi^p < \infty$  and  $E\eta^q < \infty$  , then

$$E\xi\eta \leq (E\xi^p)^{\frac{1}{p}} \cdot (E\eta^q)^{\frac{1}{q}} \tag{1.12}$$

the inequality becomes relevant.

$p=q=2$  is taken in Golder's inequality, the Cauchy-Buniakovsky inequality is derived.

Work with linear combinations of given random variables in many cases  $\xi$  have to see, for their higher order moments

$$E(a\xi + b)^k = a^k m_k + C_k^1 a^{k-1} b m_{k-1} + \dots + b^k$$

the formula can be proved.

Now higher order ( $k \geq 2$ ) absolute moments  $\beta_k$ . Let us prove the following property related to  $u$  and  $v$  with respect to variables

$$\int_{-\infty}^{\infty} [u|x|^{\frac{k-1}{2}} + v|x|^{\frac{k+1}{2}}]^2 dF(x) = \beta_{k-1} u^2 + 2\beta_k uv + \beta_{k+1} v^2 \geq 0$$

Minus didn't happen quadratic form let's see. It is quadratic form determinant counting

$$\beta_k^{2k} \leq \beta_{k-1}^k \cdot \beta_{k+1}^k$$

we form the inequality. In this inequality, if the turn  $k=1, 2, \dots$  is considered,

$$\beta_1^2 \leq \beta_2, \beta_2^4 \leq \beta_1^2 \beta_3^2, \beta_3^6 \leq \beta_2^3 \cdot \beta_4^3 \dots$$

If we multiply the resulting inequalities,

$$\beta_k^{k+1} \leq \beta_{k+1}^k \quad k=1, 2, \dots$$

inequalities come comes out 0 x irg while

$$\beta_k^{\frac{1}{k}} \leq \beta_{k+1}^{\frac{1}{k+1}}, \quad k=1, 2, \dots$$

the fact that come comes out In particular,

$$\beta_1 \leq \beta_2^{\frac{1}{2}}, \beta_2^{\frac{1}{2}} \leq \beta_3^{\frac{1}{3}}, \dots$$

And those inequalities are called Lyapunov inequalities.

In theory distribution function of  $F(x)$ . everyone in order moments

$$m_1, m_2, \dots, m_n, \dots$$

be available. These moments of the function  $F(x)$  are single-valued that determines

let's put the issue. This problem is mathematical in the analysis "problem of moments"

The following is related to the so-called general problem and its solution

results. If

$$\sum_{n=1}^{\infty} \frac{m_n}{n!} r^n < \infty \tag{1.13}$$

the series converges for some  $r > 0$ , the function  $F(x)$   $m_1, m_2, \dots, m_n, \dots$  is the only function with moments.

The dispersion (second-order central moment) of a random variable characterizes how scattered the values of this quantity are around the mean value. Based on this, we will dwell on the probabilistic meanings of higher-order moments.

If  $F(x)$  is a symmetric distribution function (i.e.  $\xi$  is a symmetric random variable), then all its moments of odd order are equal to 0 (of course, if these moments exist). B to him this is a symbol for

$$F(-x) = 1 - F(x) \quad x > 0$$

it is possible to be sure of the equality. Therefore, all moments of odd order, which are not equal to 0, can be taken as an asymmetric characteristic of the distribution. In this sense, the 3rd order moment of the given distribution is taken as the simplest asymmetry characteristic. Given the homogeneity of the scale

$$\gamma = \frac{\alpha_3}{\sigma^3}, \quad \sigma^2 = D\xi \tag{1.2.14}$$

expression of distribution asymmetry taken as the coefficient

will be done. Even order to (higher order with respect to dispersion) moments

probability can be given. For example,

$$\gamma_s = \frac{\alpha_4}{\sigma^4} - 3$$

The expression  $F(x)$  is called the excess coefficient of the distribution, which characterizes the level of "smoothness" of  $F(x)$  around the "center" (mean value).

It is not difficult to check that the moments of the given distribution exist, since this problem depends on the asymptotics of the "left residual"  $F(-x)$  and the "right residual"  $(1 - F(x))$ .  $x \rightarrow \infty$  For example,

$$\begin{aligned} F(-x) &= O(x^{-k}), \\ 1 - F(x) &= O(x^{-k}), \quad x \rightarrow \infty \end{aligned}$$

, then  $\nu < k$  all moments in the order exist for this distribution.

### Reversal formula

Har one  $F(x)$  distribution function for

$$f_\xi(t) = \int_{-\infty}^{\infty} e^{itx} p(x) dx \tag{1.15}$$

formula through determined  $f(t)$  characteristic function suitable will come This is your opinion the opposite is also appropriate, i.e distribution function characteristic function through one valuable is determined.

**Theorem a (reversal formula).**  $F = F(x)$  - distribution function and

$$f(t) = \int_{-\infty}^{\infty} e^{itx} dF(x) \tag{1.16}$$

to him suitable came characteristic function let it be

1 °) A gar  $a$  and  $b$  ( $a < b$ ) s  $F(x)$  of the function continuity points bo'lsa , in that case

$$F(b) - F(a) = \lim_{A \rightarrow \infty} \frac{1}{2\pi} \int_{-A}^A \frac{e^{-ita} - e^{itb}}{it} f(t) dt \quad (1.17)$$

2 °) If  $\int_{-\infty}^{\infty} |f(t)| dt < \infty$  if , then  $F(x)$  absolute continuously distribution function being his \_ density function

$$p(x) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} f(t) dt \quad (1.18)$$

Through the formula is expressed .

**Proof :** First  $F(x)$  absolute continuously has been without let's see .

In this case ( 1.15) to the formula according to

$$f(t) = \int_{-\infty}^{\infty} e^{itx} p(x) dx$$

and therefore The formula (1.18) is also integrable for  $f(t)$  of the function Fourier from replacement consists of (1.18 ) and the left of Eq right sides integrated , result has been in expression integration order Substituting , we find :

$$F(b) - F(a) = \int_a^b p(x) dx = \frac{1}{2} \int_a^b \left[ \int_{-\infty}^{\infty} e^{-itx} f(t) dt \right] dx = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(t) dt \left[ \int_a^b e^{-itx} dx \right] dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} \frac{e^{-ita} - e^{itb}}{it} dt$$

So this is it private without reverse formula Fourier integral transform from the result consists of Now (1.17 ) formula common without let's move on to the proof .

$$1 \circ . f_{\xi}^{\nu}(t) = i^{\nu} \int_{-\infty}^{\infty} x^{\nu} e^{itx} dF_{\xi}(x), \quad \nu = 1, 2, \dots, k$$

from the formula this

$$J_A = \frac{1}{2\pi} \int_{-A}^A \frac{e^{-ita} - e^{itb}}{it} f(t) dt = \frac{1}{2\pi} \int_{-A}^A \frac{e^{-ita} - e^{itb}}{it} \left[ \int_{-\infty}^{\infty} e^{-itx} dF(x) \right] dt \quad (1.19)$$

of equality appropriate the fact that come comes out

$$2 \circ . |e^{ix} - e^{iy}| = \left| \int_x^y e^{it} du \right| \leq \left| \int_x^y du \right| = |x - y|$$

from inequality

$$\left| \frac{e^{-ita} - e^{itb}}{it} e^{itx} \right| = \left| \frac{e^{-ita} - e^{itb}}{it} \right| \leq b - a$$

the fact that come comes out That's it with together

$$\int_{-A}^A \int_{-\infty}^{\infty} (b - a) dF(x) < 2A(b - a) < \infty$$

relationship appropriate what happened \_ for (1.19) in the integral Fubini according to the theorem integration order replacement can \_ So by doing

$$\begin{aligned}
 J_A &= \frac{1}{2\pi} \int_{-\infty}^{\infty} \left[ \int_{-A}^A \frac{e^{-ita} - e^{itb}}{it} e^{itx} dt \right] dF(x) = \\
 &= \frac{1}{2\pi} \int_{-\infty}^{\infty} \left[ \int_{-A}^A \frac{\sin t(x-a) - \sin t(x-b)}{t} dt \right] dF(x) = \\
 &= \frac{1}{2\pi} \int_{-\infty}^{\infty} \left[ \int_{-A(x-a)}^{A(x-a)} \frac{\sin z}{z} dz - \int_{-A(x-b)}^{A(x-b)} \frac{\sin z}{z} dz \right] dF(x) = \int_{-\infty}^{\infty} G_A(x) dF(x), \quad (1.2.20)
 \end{aligned}$$

this on the ground

$$G_A(x) = \frac{1}{2\pi} \left[ \int_{-A(x-a)}^{A(x-a)} \frac{\sin z}{z} dz - \int_{-A(x-b)}^{A(x-b)} \frac{\sin z}{z} dz \right] \quad (1.21)$$

$g(x, y) = \int_x^y \frac{\sin z}{z} dz$  function  $x$  and  $y$  arguments according to flat continuously and

$$\lim_{x \rightarrow -\infty, x \rightarrow \infty} g(x, y) = \pi \quad (1.22)$$

equality appropriate . From this all  $A$  and  $x$  numbers for so  $S$  a fixed number is found such that its for  $|G_A(x)| \leq C < \infty$  of inequality execution come it clicks . That's it with together , from equations (1.21) and (1.22).

$$\lim_{A \rightarrow \infty} G_A(x) = G(x)$$

of the limit existence easily to prove can \_ Here \_

$$G(x) = \begin{cases} 0, & x < a, x > b; \\ \frac{1}{2}, & x = a, x = b; \\ 1, & a < x < b. \end{cases}$$

From this and Lebesgue's Majorant approach about to the theorem according to the integral sign under  $A \rightarrow \infty$  to the limit at transition from possible using the following we find :

$$\begin{aligned}
 \lim_{A \rightarrow \infty} J_A &= \lim_{A \rightarrow \infty} \int_{-\infty}^{\infty} G_A(x) dF(x) = \int_{-\infty}^{\infty} G(x) dF(x) = \\
 &= \int_{-\infty}^a G(x) dF(x) + \int_a^b G(x) dF(x) + \int_b^{\infty} G(x) dF(x) = \\
 &F(b-) - F(a) + \frac{1}{2} [F(a) - F(a-) + F(b) - F(b-)]
 \end{aligned}$$

If  $a$  and  $b$  points of the function  $F(x)$ . interruption points that attention the last one from equality

$$f_{\xi}^{\nu}(0) = i^{\nu} M \xi^{\nu}$$

of the formula appropriate the fact that come comes out

### Literature .

- 1 . F.A. Bartenev. Non-standard problems in algebra. Moscow 1976.
- 2.I.F. \_ Sharygin, V.I. Golubev. Facultative course in mathematics. Moscow. Prosveshchenie. 1991.

3. V. V. Vavilov, N. I. Melnikov , S. N. Olexnik , P. N. Pasichenko . Zadachi po mathematics. Algebra. Spravochnoy posobie. Moscow. Science. 1987g.
4. Olechnik S.N. i dr. Uravneniya i neravenstva. Non-standard solution. 10-11 class. Teaching method . posobie. Moscow. 2001.
4. PAYZIMATOVA, M. S., ABDUNAZAROVA, D. T., & SULAYMONOV, M. M. U. (2015). THEORY I METHODOLOGY EDUCATION MATHEMATICS KAK SAMOSTOYATEL'NAYA NAUCHNAYA DISCIPLINA. In *BUDUshchEE NAUKI-2015* ( pp . 389-393).
5. ABDUNAZAROVA, D. T., PAYZIMATOVA, M. S., & SULAYMONOV, M. M. U. (2015). PROBLEMA PODGOTOVKI BUDUSHCHIX PEDAGOGOVI K INNOVATSIONNOY PEDAGOGICHESKOY DEYATEL'NOSTI. In *Molodej i XXI vek-2015* ( pp . 284-288).
6. Abdikarimov , R. A., Mansurov, M. M., & Akbarov, U. Y. (2019). Chislennoe issledovanie flattera vyazkouprugogo jestko-zashchemlennogo sterzhnya s uchetom fizicheskoy i aerodinamicheskoy nelineynostey. *Vestnik RGGU. Series: Informatics. Information security. Mathematics* , (3), 94-107.
7. Abdikarimov , R. \_ A. , Mansurov , M. \_ M. , & Akbarov , U. Y. \_ (2019). Numerical study of a flutter of a viscoelastic rigidly clamped rod with regard for the physical and aerodynamic nonlinearities. *VESTNIK RGGU* , 3 , 95.
8. Mansurov , M., & Akbarov , U. (2021). FLATTER OF VISCOELASTIC FREE OPEROUS ROD AT THE END. *Scientific Bulletin of Namangan State University* , 3 (3), 36-42.
9. Jumakulov , Kh . K. , & Salimov , M. (2016). O METODAX PROVEDENIYA I STRUKTURE PEDAGOGICHESKOGO EXPERIMENTA. *Main editor* , 80.
10. Esonov , M. M. (2013). Methodological practices in creative approach and training theory. *Vestnik KRAUNTS. Physical and mathematical science* , 7 (2), 78-83.
11. Esonov , M. M., & Zunnunova , D. T. (2020). Razvitie matematicheskogo myshleniya na urokax geometrii posredstvom zadach na issledovanie parametrov izobrazheniya. *Vestnik KRAUNTS. Physical and mathematical science* , 32 (3), 197-209.
12. Jarov, V. K., & Esonov , M. M. (2019). OBUCHENIE STUDENTOV MATHEMATIKOV NAUCHNYM METODAM ISSLEDOVANIYA NA OSNOVE RESHENIYA KOMPLEKSA GEOMETRICHESKIH ZADACH. *Continuum . Mathematics. Informatics. Education* , (4), 10-16.
13. Esonov , M. M., & Esonov , A. M. (2016). Realization methodology tvorcheskogo podhoda na zanyatiyax spetskursa po teorii izbrazheniy. *Vestnik KRAUNTS. Physical and mathematical science* , (1 (12)), 107-111.
14. Esonov , M. M. (2017). Postroenie pryamoy, perpendicular danny pryamoy. *Vestnik KRAUNTS. Physical and mathematical science* , (2 (18)), 111-116.
15. Esonov , M. M. (2016). PRAKTICHESKIE OSNOVY OBUCHENIYA METODAM ISOBRAJENIY K RESHENIYU ZADACH V KURSE GEOMETRII. In *Theory and practice of modern humanitarian and aesthetic science* ( pp . 155-159).
16. Esonov , M. M. (2014). Proektirovanie izucheniya" Metodov izobrazheniy" v kontekte tvorcheskogo pokhoda k sheniyu zadach. In *Theory and practice of modern humanitarian and aesthetic science* ( pp . 259-265).
17. Ergasheva , HM, Mahmudova , OY, & Ahmedova , GA (2020). GEOMETRIC SOLUTION OF ALGEBRAIC PROBLEMS. *Scientific Bulletin of Namangan State University* , 2 (4), 3-8.
18. Marasulova , ZA, & Rasulova , GA (2014). Information resources as a factor of integration of models and methodologies. *Vestnik KRAUNC. Physics and Mathematics Science* , (1), 75-80.



19. Mamsliyevich , TA (2022). ON A NONLOCAL PROBLEM FOR THE EQUATION OF THE THIRD ORDER WITH MULTIPLE CHARACTERISTICS. *INTERNATIONAL JOURNAL OF SOCIAL SCIENCE & INTERDISCIPLINARY RESEARCH* ISSN: 2277-3630 Impact factor: 7.429 , 11 (06), 66-73.
20. Mamsliyevich , TA (2022). ABOUT ONE PROBLEM FOR THE EQUATION OF THE THIRD ORDER WITH A NON-LOCAL CONDITION. *INTERNATIONAL JOURNAL OF SOCIAL SCIENCE & INTERDISCIPLINARY RESEARCH* ISSN: 2277-3630 Impact factor: 7.429 , 11 (06), 74-79.
21. Muydinjanov , DR (2019). Holmgren problem for Helmholtz equation with the three singular coefficients. *e-Journal of Analysis and Applied Mathematics* , 2019 (1), 15-30.
22. Mamadaliev , B. M. (1994). Asymptotic analysis of functional noun spacing .
23. Ergashev , A. A., & Tolibjonova , Sh. A. (2020). Osnovnye components of professional education of mathematics. *Vestnik KRAUNTS. Physical and mathematical science* , 32 (3), 180-196.
24. Zunnunov , R. T., & Ergashev , A. A. (2021). Zadacha tipa zadachi Bitsadze-Samarskogo dlya uravneniya smeshannogo tipa torogo roda v oblasti ellipticheskaya chast kotoroy-chetvert ploskosti. In *Fundamental and applied problems of mathematics and informatics* ( pp . 117-20).
25. Zunnunov , R. T., & Ergashev , A. A. (2016). Zadacha so smeshcheniem dlya uravneniya smeshannogo tipa torogo roda v neogranichennoy oblasti. *Vestnik KRAUNTS. Physical and mathematical science* , (1 (12)), 26-31.
26. Zunnunov , R. T., & Ergashev , A. A. (2017). KRAEVYA ZADACHA SO SMESHCHENIEM DLYA URAVNENIYA SMESHANNOGO TIPV NEOGRANICHENNOY OBLASTI. In *Actual problems of applied mathematics and physics* ( pp . 92-93).
27. Zunnunov , R. T., & Ergashev , A. A. (2016). Zadacha so smeshcheniem dlya uravneniya smeshannogo tipa torogo roda v neogranichennoy oblasti. *Vestnik KRAUNTS. Physical and mathematical science* , (1 (12)), 26-31.
28. Zunnunov , RT, & Ergashev , AA (2016). PROBLEM WITH A SHIFT FOR A MIXED-TYPE EQUATION OF THE SECOND KIND IN AN UNBOUNDED DOMAIN. *Bulletin KRASEC. Physical oath Mathematical Sciences* , 12 (1), 21-26.
29. Ergashev , A. A., & Talibjanova , Sh. A. (2015). Bitsadze-Samarskogo method of solution for elliptic tip and half-pole . In *Theory and practice of modern humanitarian and aesthetic science* ( pp . 160-162).
- Alyaviya , O., Yakovenko, V., Ergasheva , D., Usmanova, Sh., & Zunnunov , Kh. (2014). Evaluation of the intensity and structure of dental caries and students with normal and low functional salivary gel. *Dentistry* , 1 (3-4 (57-58)), 34-38.
30. Marasulova , Z. A., & Rasulova, G. A. (2014). The information resource is a factor integration model and method. *Vestnik KRAUNTS. Physical and mathematical science* , (1 (8)), 75-80.
31. Rasulova, G. A., Ahmedova , Z. S., & Normatov , M. (2016). METHODIKA IZUCHENIYA MATHEMATICHESEKIH TERMINOV NA ANGLYSKOM YAZYKE V PROTSESSE OBUCHENIYA. *Uchenyy XXI veka* , 65.
32. Rasulova, G. A., Ahmedova , Z. S., & Normatov , M. (2016). EDUCATION ISSUES LEARN ENGLISH LANGUAGE IN TERMS OF PROCESSES. *Uchyonyy XXI veka* , (6-2 (19)), 62-65.
33. Rasulova , G. (2022). CASE STATE AND TECHNOLOGY OF USING NON-STANDARD TESTS IN TEACHING GEOMETRY MODULE. *Eurasian journal of Mathematical theory oath computer sciences* , 2 (5), 40-43.

34. Ergasheva , HM, Mahmudova , OY, & Ahmedova , GA (2020). GEOMETRIC SOLUTION OF ALGEBRAIC PROBLEMS. *Scientific Bulletin of Namangan State University* , 2 (4), 3-8.
35. Muydinjanov , Z., & Muydinjanov , D. (2022). INFORMATION, COMMUNICATION AND TECHNOLOGY (ICT) IS FOR TEACHER AND STUDENT.
36. Muydinjanov , Z., & Muydinjanov , D. (2022). VIRTUAL LABORATORIES. *Eurasian Journal of Academic Research* , 2 (6), 1031-1034.
37. Muydinjanov , DR (2019). Holmgren problem for Helmholtz equation with the three singular coefficients. *e-Journal of Analysis and Applied Mathematics* , 2019 (1), 15-30.
38. Rahmatullaev , MM, Rafikov , FK, & Azamov , S. (2021). On the Constructive Description of Gibbs Measures for the Potts Model on a Cayley Tree. *Ukrainian Mathematical Journal* , 73 (7), 1092-1106.
39. Rahmatullaev , M., Rafikov , F. K. , & Azamov , SK (2021). Pro constructive opisi mır Gıbbssa dlya model Pottsna na dereví Come on . *Ukraine \_ \_ Matematychnyi Journal* , 73 (7), 938-950.
40. Petrosyan , VA, & Rafikov , FM (1980). Polarographic study of aliphatic nitro compounds. *Bulletin of the Academy of Sciences of the USSR, Division of chemical science* , 29 (9), 1429-1431.
41. Formanov , SK, & Jurayev , S. (2021). On Transient Phenomena in Branching Random Processes with Discrete Time. *Lobachevskiy Journal of Mathematics* , 42 (12), 2777-2784.
42. Nosirov , SN, Aroyev , DD, Sobirov , AA, & Umirzakova , MB (2022). Mutual Value Reflection and Automorphisms . *Specialist Ugdymas* , 1 (43), 2450-2454.
43. Nasirovich , NS, Davronovich , AD, & Abdurashid Ogli , SA (2021). SOME PROPERTIES OF THE DISTANCE BETWEEN TWO POINTS. *Journal of Ethics and Diversity in International Communication* , 1 (1), 54-56.
44. Sulaymanov , MMOGL (2022). ORGANIZING A LECTURE COURSE ON THE SUBJECTS OF PLANIMETRY USING THE GEOGEBRA SOFTWARE. *Central Asian Research Journal for Interdisciplinary Studies (CARJIS)* , 2 (6), 35-40.