

SOME SECOND ORDER DIFFERENTIAL EQUATIONS FUNCTIONALLY INVARIANT SOLUTIONS

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ABSTRACT

This article is devoted to the search for functionally invariant solutions of some second-order differential equations .

The search for functionally invariant solutions of differential equations is one of the main methods for constructing solutions. The problem of finding a functionally invariant solution of second-order linear differential equations was studied in the works of I. Jacobi, A. R. Forit, W. Burnside, and others in the middle of the 19th century.

In 1932, V.I. Smirnov and S.L. Sobolev were the first to apply the functionally invariant solution of wave equations to solve a specific problem of mathematical physics.

Further development of the functionally invariant solution method is associated with the name of N.P. Erugin and M.M. Smirnov. Necessary and sufficient conditions for the existence of a functionally invariant solution of differential equations of the second and fourth order with two independent variables are obtained.

second order in a finite one-link field D of the plane xOy

$$a_{11}u_{xx} + 2a_{12}u_{xy} + a_{22}u_{yy} + a_{13}u_x + a_{23}u_y = 0 \quad (1)$$

Let's look at the equation. here $a_{11}, a_{12}, a_{22} \in C^2(D)$, $a_{13}, a_{23} \in C^1(D)$ - given functions.

$u(x, y) \in C^2(D)$ the function is a solution to equation (1) and is arbitrary

a function with a continuous derivative up to the 2nd order $F(u)$ also satisfies equation (1), then such a $u(x, y)$ function is called a functionally invariant solution of equation (1).

If $u(x, y)$ (1) is a functionally invariant solution, then

$$a_{11}u_x^2 - 2a_{12}u_xu_y + a_{22}u_y^2 = 0 \quad (2)$$

is also a solution to the characteristic equation. Conversely, if it $u(x)$ satisfies equations (1) and (2), then this is a functionally invariant solution of equation (1). Thus, the problem of finding a functionally invariant solution to equation (1) is reduced to solving the system of equations (1) and (2).

Below we will deal with finding functionally invariant solutions of some differential equations.

one.

$$(\sin^2 y)u_{xx} - u_{yy} + \lambda u_x = 0 \quad (3)$$

find a functionally invariant solution of the equation. Here λ is an arbitrary constant. According to the definition of functionally invariant solutions, equation (3) and its corresponding

$$(\sin^2 y)u_x^2 - u_y^2 = 0 \quad (4)$$

it is necessary to find a joint solution of the characteristic equation.

(4) equation

$$(\sin y)u_x - u_y = 0, \quad (\sin y)u_x + u_y = 0 \quad (5)$$

can be divided into equalities.

(5) complete integrals of the equations, respectively

$$u = x - \cos y, u = x + \cos y$$

have a form that satisfies (3).

Using these

$$u = F_1(x - \cos y), u = F_2(x + \cos y) \quad (6)$$

we are building functions. Functions (6) include all solutions of equation (5).

found equations (6) twice in x and y

$$u_x = F_1'(x - \cos y),$$

$$u_{xx} = F_1''(x - \cos y),$$

$$u_y = F_1'(x - \cos y) \sin y,$$

$$u_{yy} = F_1''(x - \cos y) \sin^2 y + F_1'(x - \cos y).$$

$$u_x = F_2'(x + \cos y),$$

$$u_{xx} = F_2''(x + \cos y),$$

$$u_y = -F_2'(x + \cos y) \sin y,$$

$$u_{yy} = F_2''(x + \cos y) \sin^2 y - F_2'(x + \cos y) \cos y.$$

Substituting the found expressions into derivative equations (3),

$$\lambda_1 = -\cos y, \quad \lambda_2 = \cos y \quad (8)$$

we will produce

Thus, when equality (8) is satisfied, formula (6) gives the general solution of the system of equations (3) and (4).

$\lambda = \pm \cos y$ the function satisfies (3) at Therefore $u = F(x \pm \cos y)$, the function is a $u = x \pm \cos y$ functionally $(\sin^2 y)u_{xx} - u_{yy} \pm (\cos y)u_x = 0$ invariant solution of the equation.

2.

$$(\sin^2 y)u_{xx} - (\cos^2 x)u_{yy} + \alpha(\sin x)u_x + \alpha(\cos y)u_y = 0 \quad (9) \quad (9) \text{ find a}$$

functionally invariant solution of the equation.

In this equation, α also does not change arbitrarily. (9) - characteristic equation

$$(\sin^2 y)u_x^2 - (\cos^2 x)u_y^2 = 0 \quad (10)$$

looks like Divide also (10) into two equalities, as above:

$$(\sin y)u_x - (\cos x)u_y = 0, \quad (\sin y)u_x + (\cos x)u_y = 0 \quad (11)$$

Complete integrals (11).

$$u = \sin x + \cos y$$

will have an appearance.

As above, we get the following function from this equation

$$u = F(\sin x + \cos y) \quad (12)$$

the last equation we can multiply x and y twice.

$$u_x = F'(\sin x + \cos y) \cos x,$$

$$u_{xx} = F''(\sin x + \cos y) \cos^2 x - F'(\sin x + \cos y) \sin x,$$

$$u_y = -F'(\sin x + \cos y) \sin y,$$

$$u_{yy} = F''(\sin x + \cos y) \sin^2 y - F'(\sin x + \cos y) \cos y.$$

Substituting the found expressions into derivative equations (9),

$$\alpha = \frac{\sin^2 y \sin x + \cos^2 x \cos y}{\sin x \cos x - \cos y \sin y}, \quad (13)$$

find the value. When the last equality is satisfied, (12) is a general solution of (9) and (10).

So $u = \sin x + \cos y$ function

$$(\sin^2 y)u_{xx} - (\cos^2 x)u_{yy} + \frac{\sin^2 y \sin x + \cos^2 x \cos y}{\sin x \cos x - \cos y \sin y} (\sin x)u_x + \frac{\sin^2 y \sin x + \cos^2 x \cos y}{\sin x \cos x - \cos y \sin y} (\cos y)u_y = 0$$

functionally - invariant solution of the equation.

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